

## Representations of $\{3\}$ , $\{4\}$ , $\{1, 3\}$ , $\{1, 4\}$ Inverses

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ABSTRACT. In this paper we obtain a general solution of the Penrose's equation (3), solution of the equation (4) and a general solution of the system of Penrose's equations (1),(3) and (1),(4). We also introduce a determinantal representation of the classes of  $\{3\}$ ,  $\{4\}$ ,  $\{1, 3\}$  and  $\{1, 4\}$ -inverses of complex matrices.

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